

HW #1 - due Fri 11/6

- Read Ch 1
- Ch 1 Review Problems pp. 36-38 #1-30

Quiz #1 - Thur, 11/12

- Vocab
- Fill in the blank proofs

HW #2 - due Fri, 11/13

- Read Ch 2
- Ch 2 Review Problems pp. 71-74 #1-19, 31-49

HW #3 - due Wed, 11/18

- Read Ch 3
- Ch 3 Review Problems pp. 124-128 #17-31, 34-49

Test #1 - Thur, 11/19

3.5 – Complementary and Supplementary Angles

Def: Two angles are complementary iff their sum is 90° .

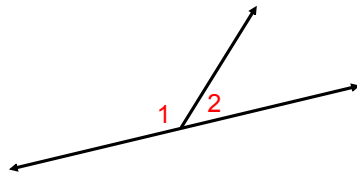
Def: Two angles are supplementary iff their sum is 180° .

Theorem 3: Complements of the same angle are equal. (proved on p.106)

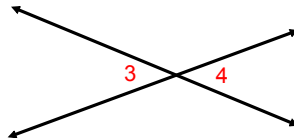
Theorem 4: Supplements of the same angle are equal.

3.6 – Linear Pairs and Vertical Angles

Def: Two angles are a linear pair iff they have a common side and their other sides are opposite rays.



Def: Two angles are vertical angles iff the sides of one angle are opposite rays to the sides of the other.



Theorem 5: The angles in a linear pair are supplementary.

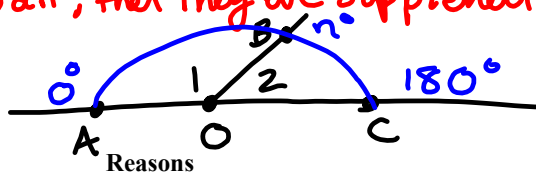
If 2 angles are a linear pair, then they are supplementary.
 Given: $\angle 1$ and $\angle 2$ are a linear pair.

Prove: $\angle 1$ and $\angle 2$ are supplementary.

Proof:

Statements

1. $\angle 1$ and $\angle 2$ are a linear pair.
2. Rays OA and OC are opposite rays.
3. Let the coordinates of OA, OB, and OC be 0, n, and 180.
4. $\angle 1 = n - 0 = n^\circ$ and $\angle 2 = (180 - n)^\circ$
5. $\angle 1 + \angle 2 = n^\circ + (180 - n)^\circ = 180^\circ$
6. $\angle 1$ and $\angle 2$ are supplementary.



Reasons
Given

If two angles are a linear pair, they have a common side and their other sides are opposite rays.

Protractor postulate
Protractor postulate

Addition

Two angles are supplementary if their sum is 180° .

Theorem 6: Vertical angles are equal.

3.7 – Perpendicular and Parallel Lines

Def: Two lines are **perpendicular** iff they form a right angle.

Theorem 7: Perpendicular lines form four right angles.

Corollary to the definition of a right angle: All right angles are equal.

Theorem 8: If the angles in a linear pair are equal, then their sides are perpendicular.

Def: Two lines are **parallel** iff they lie in the same plane and do not intersect.

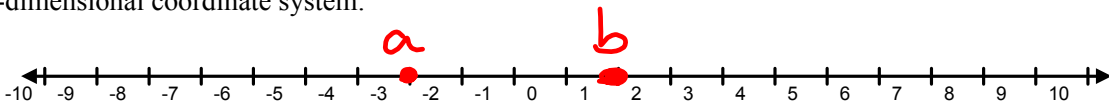


Chapter 4 – Congruence

4.1 – Coordinates & Distance

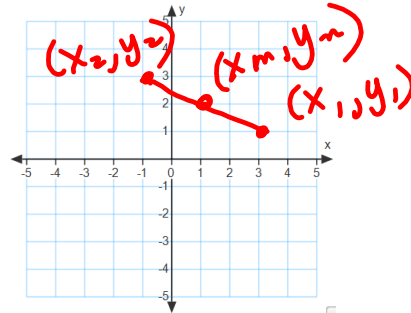
$$d(a,b) = |b-a| = |a-b| = -1 - (-3) = 4$$

one-dimensional coordinate system:



two-dimensional coordinate system:

Origin, axes, quadrants, coordinates

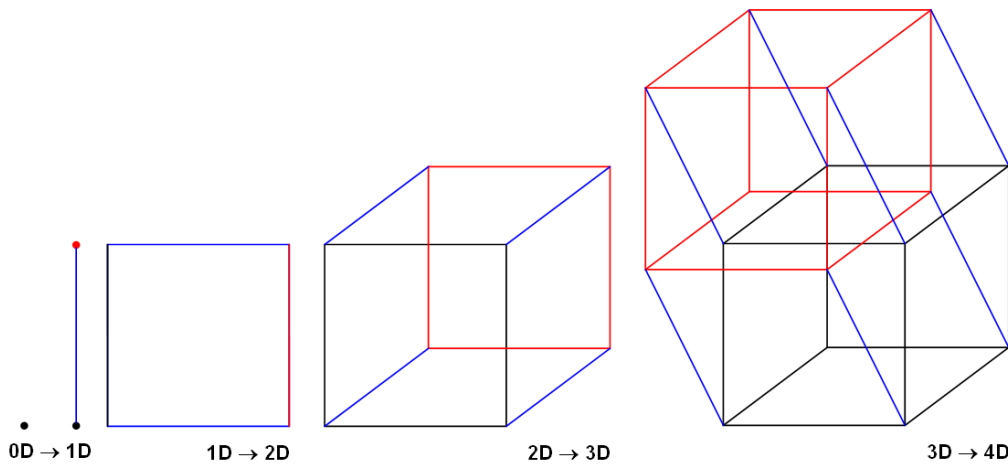


Distance formula:

The distance between the points $P_1(x_1, y_1)$ and $P_2(x_2, y_2)$ is

$$\sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

midpoint : $\left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right)$

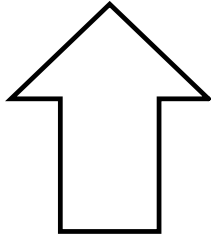
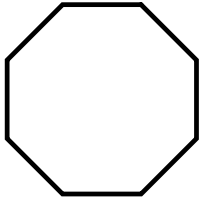


4.2 – Polygons and Congruence

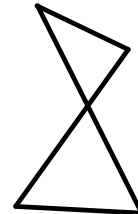
Def: A **polygon** is a connected set of at least three line segments in the same plane such that each segment intersects exactly two others, one at each endpoint.

The line segments are the sides of the polygon, and the endpoints are its vertices. The number of sides and vertices is always the same, and the polygon is referred to as an “ n -gon” if it has n sides and n vertices.

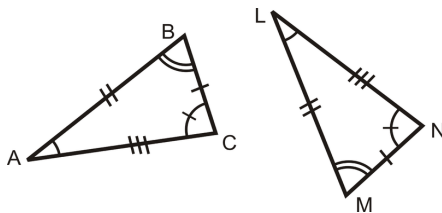
Polygons:



Not Polygons:



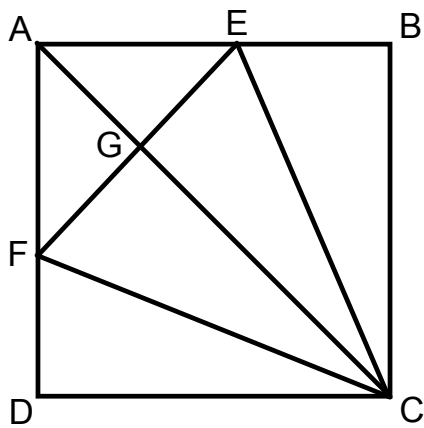
Def: Two triangles are **congruent** iff there is a correspondence between their vertices such that all of their corresponding sides and angles are equal.



$$\triangle ABC \cong \triangle LMN$$

\cong means “is congruent to”

$$ABC \leftrightarrow LMN$$



Name the triangles that appear to be congruent to the following triangles.

12. $\triangle AFG \cong \triangle AEG$

13. $\triangle ACD \cong \triangle ACB$

14. $\triangle CDF \cong \triangle CBE$

15. $\triangle ACE \cong \triangle ACF$

16. Name a triangle that is not congruent to any other triangle in the figure.

$\triangle CFE$; $\triangle AFE$

Corollary to the definition of congruent triangles: Two triangles congruent to a third triangle are congruent to each other.

55. Give the reasons for the statements in the proof.

Given: $\triangle ABC \cong \triangle XYZ$ and $\triangle DEF \cong \triangle XYZ$

Prove: $\triangle ABC \cong \triangle DEF$

Proof:

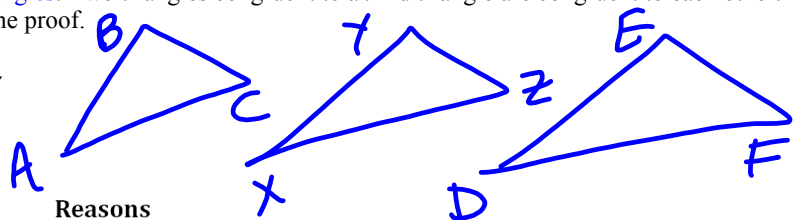
Statements

1. $\triangle ABC \cong \triangle XYZ$ and $\triangle DEF \cong \triangle XYZ$

2. $\angle A = \angle X, \angle B = \angle Y, \angle C = \angle Z$
 $\underline{AB} = \underline{XY}, \underline{BC} = \underline{YZ}, \underline{AC} = \underline{XZ}$
 $\angle D = \angle X, \angle E = \angle Y, \angle F = \angle Z$
 $\underline{DE} = \underline{XY}, \underline{EF} = \underline{YZ}, \underline{DF} = \underline{XZ}$

3. $\angle A = \angle D, \angle B = \angle E, \angle C = \angle F$
 $\underline{AB} = \underline{DE}, \underline{BC} = \underline{EF}, \underline{AC} = \underline{DF}$

4. $\triangle ABC \cong \triangle DEF$

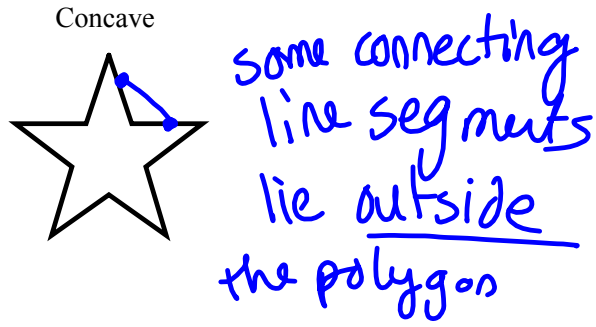
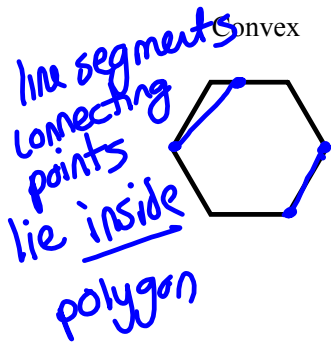


Reasons

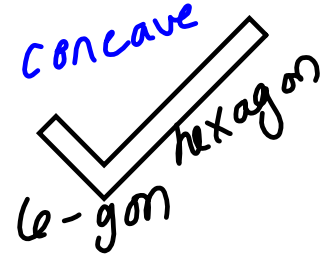
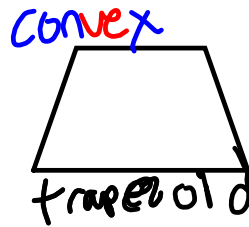
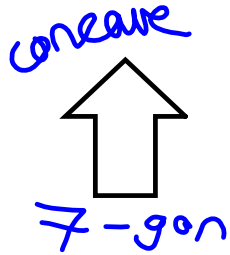
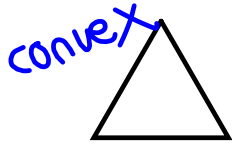
Given

Def. of congruent triangles

Substitution (all the things
 Def. of congruent \triangle 's in #2)



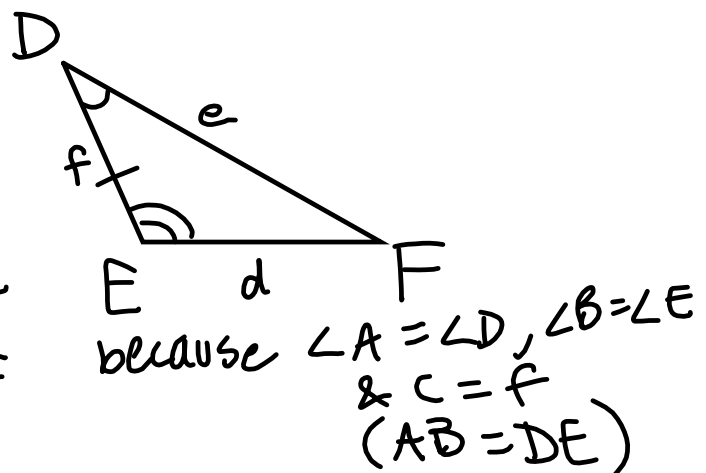
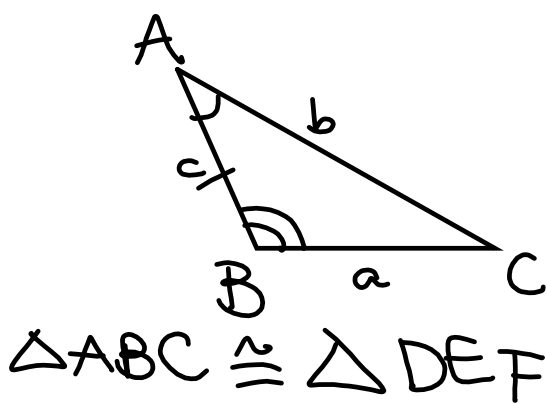
Convex or concave?



4.3 – ASA and SAS Congruence

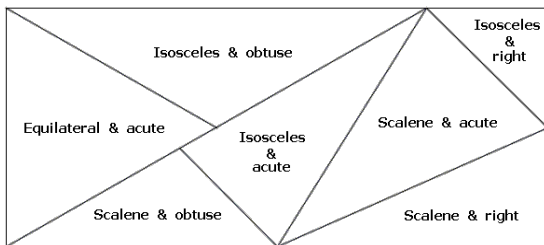
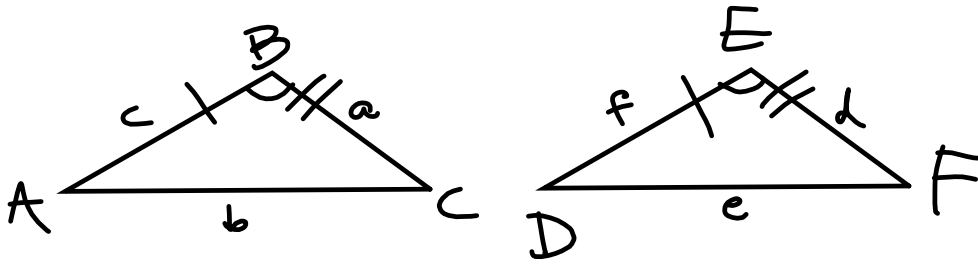
Postulate 5: The ASA Postulate

If two angles and the included side of one triangle are equal to two angles and the included side of another triangle, the triangles are congruent.



Postulate 6: The SAS Postulate

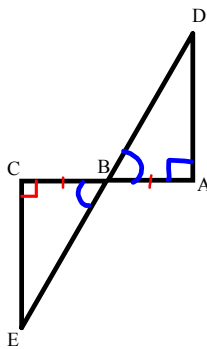
If two sides and the included angle of one triangle are equal to two sides and the included angle of another triangle, the triangles are congruent.



- 16. Equilateral - all equal sides
- 17. Acute - all 3 \angle 's are acute
- 18. Isosceles - 2 equal sides (& 2 equal angles)
- 19. Obtuse - 1 obtuse angle
- 20. Scalene - no equal sides or angles
- 21. Right - 1 right angle

4.4 – Congruence Proofs

Def: Corresponding parts of congruent triangles are equal.



Given: $CA \perp AD, CB = BA,$
 $\angle C$ is a right angle and
 $\angle CBE$ and $\angle DBA$ are vertical angles.

Prove: $CE = AD$

1. $CA \perp AD,$
 $CB = BA$
 $\angle C$ is right
 $\angle CBE$ & $\angle DBA$ are vertical
2. $\angle CBE = \angle DBA$
3. $\angle A$ is a right angle
4. $\angle A = \angle C$
5. $\triangle CBE \cong \triangle DBA$
6. $CE = AD$

Given

vertical angles
 are equal
 perpendicular lines
 meet @ right angles
 all right \angle 's are
 equal

ASA congruence
 corresponding parts of
 congruent \triangle 's are equal