

HW #4 - Due Fri, Dec 4
 Ch 4 Review Problems pp.176-180 #7-36, 48,51,52

Khan Academy exercises: "Congruence"

HW #5 - Due Fri, Dec 11
 Ch 5 Review Problems pp. 206-209 #15-50

HW #6
 Ch 6

Test #2 - Mon 12/14 or Wed. 12/16?

The "Whole Greater than Part" Theorem: If $a > 0$, $b > 0$, and $a + b = c$, then $c > a$ and $c > b$

Proof:

Statements

Reasons

1. $a > 0$ and $b > 0$

Given

2. $a + b > b$ and $a + b > a$

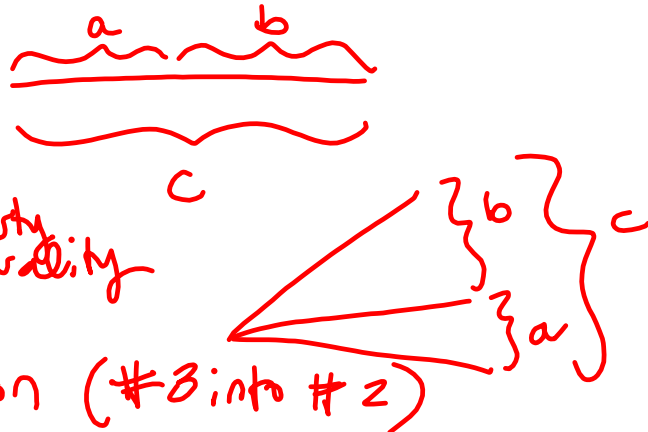
Addition Property of Inequality

3. $a + b = c$

Given

4. $c > b$ and $c > a$

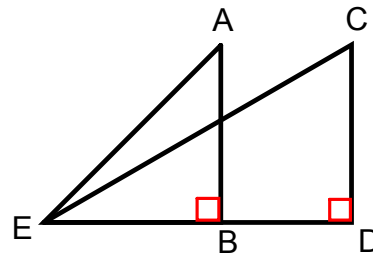
Substitution (#3 into #2)



47.

Given: $AB=CD$; $EA=EC=ED$

Prove: $\angle AED > \angle CED$



Proof:

Statements

1. $EA=EC=ED$

2. $\angle AED = \angle AEC + \angle CED$
 $a < c < d$

3. $\angle AEC > 0$

4. $\angle AED > \angle CED$

Reasons

Given

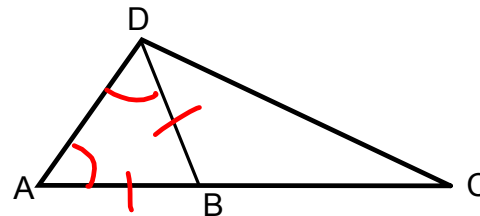
Betweenness of Rays Theorem
 betweenness of rays def'n
 Protractor Postulate

Whole is Greater than Part

48.

Given: $A-B-C$; $\angle ADB = \angle DAB$

Prove: $AC > DB$



Proof:

Statements:

1. $A-B-C$ &
 $\angle ADB = \angle DAB$

2. $AB = DB$

3. $AC > AB$
 $\{ AB > 0$

4. $AC > DB$

Reasons:

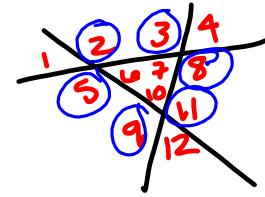
Given

If 2 \angle 's in a Δ are $=$, then
 the sides opposite them are $=$

Whole Greater than Part
 Protractor Postulate
 Substitution (#2 into #3)

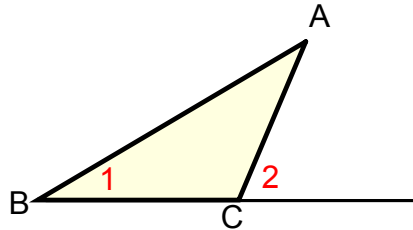
5.2 – The Exterior Angle Theorem

Def: An exterior angle of a triangle is an angle that forms a linear pair with an angle of the triangle.



In $\triangle ABC$, exterior $\angle 2$ forms a linear pair with $\angle ACB$.

The other two angles of the triangle, $\angle 1$ ($\angle B$) and $\angle A$ are called remote interior angles with respect to $\angle 2$.



Theorem 12: The Exterior Angle Theorem

An Exterior angle of a triangle is greater than either remote interior angle.

Given: $\angle ACD$ is an exterior angle of $\triangle ABC$.
 Prove: $\angle ACD > \angle A$ and $\angle ACD > \angle B$

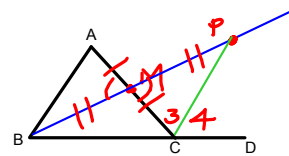
Proof:

Statements

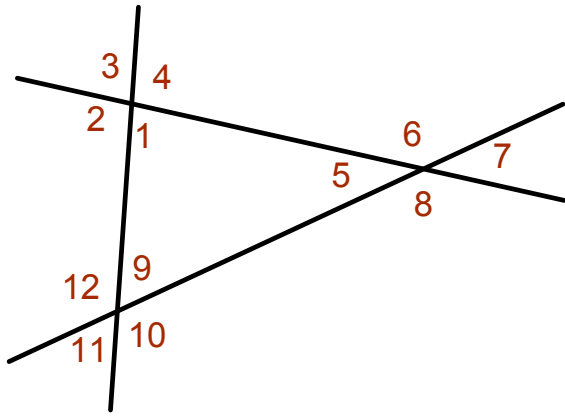
1. $\angle ACD$ is an exterior angle of $\triangle ABC$
2. Let M be the midpoint of AC
3. $AM = MC$
4. Draw line BM
5. Choose P on line BM so that $MB = MP$
6. Draw CP
7. $\angle AMB = \angle CMP$
8. $\triangle AMB \cong \triangle CMP$
9. $\angle A = \angle 3$
10. $\angle ACD = \angle 3 + \angle 4$
11. $\angle ACD > \angle 3$
12. $\angle ACD > \angle A$

Reasons

Given
 Compass construction / uniqueness of midpoint
 midpoint divides the segment into 2 equal parts
 2 points determine a line
 Ruler Postulate
 2 points determine a line
 Vertical angles are equal
 SAS congruency
 Corresponding parts of Congruent \triangle s are equal
 Betweenness of Rays Theorem
 Whole is Greater than Part
 Substitution (#9 & 12)



Case for $\angle B$ is similar.



31. What does the result in exercise 30 indicate about the sum of the exterior angles of a triangle?

always = 720°

Find each of the following sums.

26. $\angle 1 + \angle 2 + \angle 3 + \angle 4$

360°

27. $\angle 1 + \angle 2 + \angle 3 + \angle 4 + \angle 5 + \angle 6 + \angle 7 + \angle 8 + \angle 9 + \angle 10 + \angle 11 + \angle 12$

$3(360^\circ) = 1080^\circ$

28. $\angle 1 + \angle 5 + \angle 9$

180° (Δ sum Thm)

29. $\angle 3 + \angle 7 + \angle 11$

180° (vertical \angle 's are \cong & subst. w/ #28)

30. $\angle 2 + \angle 4 + \angle 6 + \angle 8 + \angle 10 + \angle 12$

$720^\circ = 1080^\circ - 180^\circ - 180^\circ$
(#27 - (#28 & 29))