

1. Rewrite in set-builder notation:

$$[-3, 5) = \{x \mid -3 \leq x < 5\}$$

2. Rewrite in interval notation:

$$\{x \mid x \leq 2\} = (-\infty, 2]$$

Solve for x (leave any fractional answers as improper fractions, not mixed num)

$$3 \cdot \left(\frac{1}{3}(x-7) + 5\right) = 6x + 4$$

$$x - 7 + 15 = 18x + 12$$

$$x + 8 = 18x + 12$$

$$-4 = 17x$$

$$\frac{-4}{17} = x$$

4. Set up a table and write an equation, but do not solve:

How much water must be evaporated from 10 gallons of a 12% sugar solution in order to obtain a 15% sugar solution?

Liquid	volume of sol'n (gal)	% conc. sugar	volume of sugar
12% water	10	0.12	1.2
x		0	0
15% water	10-x	0.15	0.15(10-x)

$$1.2 = 0.15(10-x)$$

2.5 Inequalities in One Variable

10. $5x + 2 \geq 4x - 1$

$$\{x \mid x \geq -3\} = [-3, \infty)$$

$$(-1) \cdot 3 \geq -x \cdot (-1)$$

$$-3 \leq x \leftrightarrow x \geq -3$$

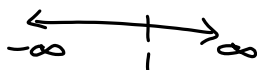
26. $2 - 5(x + 1) \geq 3(x - 1) - 8$

$$2 - 5x - 5 \geq 3x - 3 - 8$$

$$-5x - 3 \geq 3x - 11$$

$$\frac{-8x}{-8} \geq \frac{-8}{-8}$$

$$\{x \mid x \leq 1\} = (-\infty, 1]$$



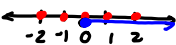
Compound Inequalities

and \cap intersection $A \cap B$

x is in both A and B




or \cup union $A \cup B$

x is in either A or B

$A = \{x | x \geq 0\}$ $\mathbb{R}, \mathbb{Q}, \mathbb{Z}, \mathbb{N}, \emptyset$
 $Z \cap A = \text{whole numbers}$
 $\{0, 1, 2, 3, \dots\}$ 
 $B = [-5, 4)$ $C \cap B = C - B = \{4, 5\}$
 $C = \{1, 2, 3, 4, 5\}$ $D \cup \mathbb{Q} = \mathbb{Q}$
 $D = \{-1, -3, \frac{1}{2}, \frac{2}{3}\}$ $E \cap A = \{\pi\}$
 $E = \{-\sqrt{2}, \pi\}$

$A = \{x | x \geq 0\}$ $\mathbb{R}, \mathbb{Q}, \mathbb{Z}, \mathbb{N}, \emptyset$
 $B \cap \mathbb{N} =$
 $D \cap A =$
 $B \cup E =$
 $C = \{1, 2, 3, 4, 5\}$ $A \cup C =$
 $D = \{-1, -3, \frac{1}{2}, \frac{2}{3}\}$ $E \cap \mathbb{Q} =$
 $C \cap \mathbb{Z} =$
 $E = \{-\sqrt{2}, \pi\}$ $B \cap A =$

$-2 < x < 3$
 $-2 < x \text{ and } x < 3$

$x \leq 3$ $x > 0$	or \cup	and \cap
	$(-\infty, \infty) = \mathbb{R}$	$(0, 3] = \{x 0 < x \leq 3\}$
	$[-1, \infty) = \{x x \geq -1\}$	$(2, \infty) = \{x x > 2\}$
	$(-\infty, 2] \cup (3, \infty)$ $\{x x \leq 2 \text{ or } x > 3\}$	\emptyset

1. Forty liters of pure maple syrup that cost \$9.00 per liter were mixed with imitation maple syrup that cost \$4.25 per liter. How much imitation maple syrup is needed to make a mixture to sell for \$5.50 per liter?

Syrup type	volume of syrup (L)	cost per liter	total cost
pure	40	\$9	40(9)
imitation	x	\$4.25	x(4.25)
mixture	40+x	\$5.50	(40+x)(5.5)

$$40(9) + 4.25x = 5.5(40+x)$$

$$360 + 4.25x = 220 + 5.5x$$

$$140 = 1.25x$$

$$\frac{14000}{125} = \frac{100}{100} \cdot \frac{140}{1.25} = x$$

$$\begin{array}{r} 112 \\ 125 \overline{)14000} \\ \underline{125} \\ 1500 \\ \underline{1250} \\ 250 \end{array}$$

112 Liters of imitation maple syrup

2. How many milliliters of pure acid must be added to 60 ml of a 30% acid solution to make a 50% acid solution?

solution type	volume of solution (mL)	concentration	volume of dissolved substance
30% sol'n	60	0.30	60(0.3)
pure acid	x	1.00	x(1)
50% sol'n	60+x	0.50	(60+x)(0.5)

$$60(0.3) + x = 0.5(60+x)$$

$$18 + x = 30 + 0.5x$$

$$0.5x = 12$$

$$x = \frac{12}{0.5} = \frac{120}{5} = 24$$

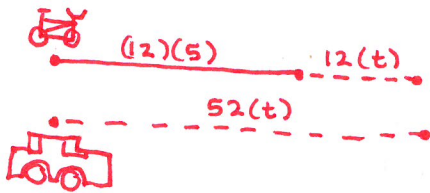
$$2 \cdot \frac{1}{2}x = 12 \cdot 2$$

$$x = 24$$

24 mL of pure acid

3. A car traveling 52 miles per hour overtakes a cyclist who, riding at 12 miles per hour, has a 5-hour head start. How far from the starting point does the car overtake the cyclist?

vehicle	rate (mph)	x time (h)	= distance (mi)
car	52	t	52(t)
cyclist	12	t+5	12(t+5)



$$52(t) = 12(t+5)$$

$$52t = 12t + 60$$

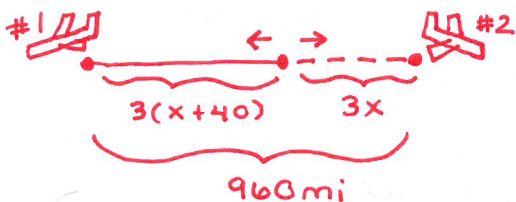
$$40t = 60$$

$$t = \frac{60}{40} = \frac{3}{2}$$

$$\text{distance} = 52\left(\frac{3}{2}\right) = \boxed{78 \text{ miles}}$$

4. Two planes start from the same point and fly in opposite directions. The first plane is flying 40 miles per hour faster than the second plane. In 3 hours, the planes are 960 miles apart. Find the speed of each plane.

plane	rate (mph)	x time (h)	= distance (mi)
1	$x+40$	3	$3(x+40)$
2	x	3	$3x$



$$3(x+40) + 3x = 960$$

$$3x + 120 + 3x = 960$$

$$6x = 840$$

$$x = \frac{840}{6} = 140$$

plane #1 travels at 180 miles per hour
plane #2 travels at 140 miles per hour