

Review:

An industrial pulley has a 60 inch diameter, and moves a belt at a rate of 60 miles per hour. What is the angular speed of a point on the edge of the pulley?

$r = 30 \text{ in}$   
 $v = 60 \text{ mi/h}$   
 $\omega = ? \text{ rev/min}$

*in rev/min*

$\frac{v}{r} = \frac{r\omega}{r}$   
 $\omega = v \cdot \frac{1}{r}$

$\omega = \frac{60 \text{ mi}}{\text{h}} \cdot \frac{1}{30 \text{ in}} \cdot \frac{12 \text{ in}}{1 \text{ ft}} \cdot \frac{5280 \text{ ft}}{1 \text{ mi}} \cdot \frac{1 \text{ k}}{60 \text{ min}} \cdot \frac{1 \text{ rev}}{2\pi}$

$= \frac{1056 \text{ rev}}{\pi} \text{ /min}$

Find the exact value of the following.

- a.  $\cos 270^\circ = \boxed{0}$
- b.  $\sin -225^\circ = \boxed{\frac{1}{\sqrt{2}}}$
- c.  $\csc 315^\circ = \boxed{-\sqrt{2}}$
- d.  $\sec 420^\circ = \boxed{2}$
- e.  $\tan -135^\circ = \boxed{1}$

**Graphing Trigonometric Functions** continued...

**Goal:** Transform a trigonometric function of the form  $y = f(x)$  to one of the form  $y = af(bx + c) + d$  by observing changes in amplitude and period, as well as horizontal and vertical shifts.

**Recall:**

- Constants that are multiplied (divided) result in a stretching/scaling of the graph (amplitude/period changes), that we show by changing the scale on our axes
- Constants that are added (subtracted) result in shifting of the graph
- Constants outside the function ( $a$  &  $d$ ) affect it vertically, as we would expect
- Constants inside the function ( $b$  &  $c$ ) affect it horizontally, opposite of what we would expect

**Note:**

When both  $b$  and  $c$  are present (i.e. when  $b$  is anything other than 1), the horizontal shift is not just  $c = \frac{c}{1}$ , as it is affected by the presence of  $b$ . In this case (and in general), the horizontal shift is  $\frac{c}{b}$ , which we can more easily see by factoring  $b$  out in the general

equation:  $y = af\left[b\left(x + \frac{c}{b}\right)\right] + d$

Summary:

For a Trigonometric function of the form  $y = af \left[ b \left( x + \frac{c}{b} \right) \right] + d$ ,

Amplitude =  $|a|$  (note that amplitude is always positive)

Period =  $\frac{\text{original period of the function } (\pi \text{ or } 2\pi)}{|b|}$

Horizontal shift =  $\frac{c}{b}$ , left if  $\frac{c}{b} > 0$ , right if  $\frac{c}{b} < 0$  "phase shift" =  $-\frac{c}{b}$

Vertical shift =  $d$ , up if  $d > 0$ , down if  $d < 0$

$y = -\frac{1}{2} \sin \pi x + \frac{3}{2}$

amplitude:

$\frac{1}{2}$

period:

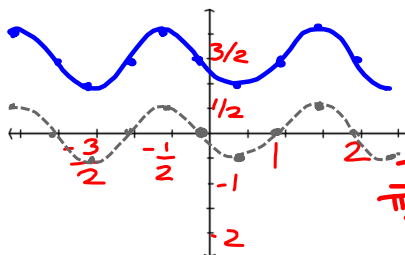
$\frac{2\pi}{\pi} = 2$

horiz. shift:

0 (none)

vert. shift:

$+3/2$   
up  $3/2$



$y = 2 \sec \left( \frac{\pi}{2} x - \pi \right)$

amplitude:

2

period:

$\frac{2\pi}{\pi/2} = \frac{2\pi}{1} \cdot \frac{2}{\pi} = 4$

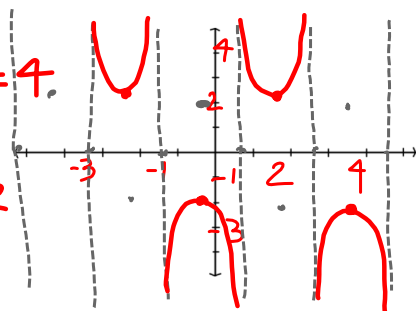
horiz. shift:

right  
 $\frac{\pi/2}{\pi/2} = \frac{\pi}{1} \cdot \frac{2}{\pi} = 2$

vert. shift:

0

$y = -2 \sec \frac{\pi}{2} x$



$y = -\frac{1}{3} \tan \left( \frac{1}{4} x + \frac{\pi}{4} \right) - \frac{1}{3}$

amplitude:

$\frac{1}{3}$

period:

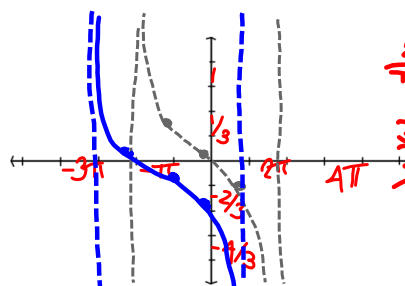
$\frac{\pi}{1/4} = 4\pi$

horiz. shift:

$\frac{\pi/4}{1/4} = \frac{\pi}{1} \cdot \frac{1}{4} = \frac{\pi}{4}$  left

vert. shift:

down  $\frac{1}{3}$



$y = -2 \cos \left( \frac{\pi}{3} x - \frac{3\pi}{2} \right) + 1$

amplitude:

2

period:

$\frac{2\pi}{\pi/3} = 6$

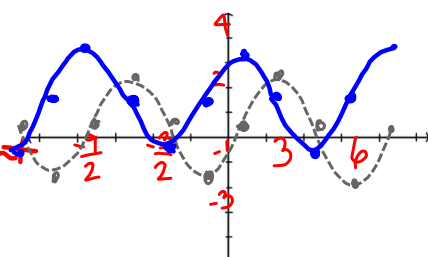
horiz. shift:

$\frac{3\pi/2}{\pi/3} = \frac{9}{2}$  right

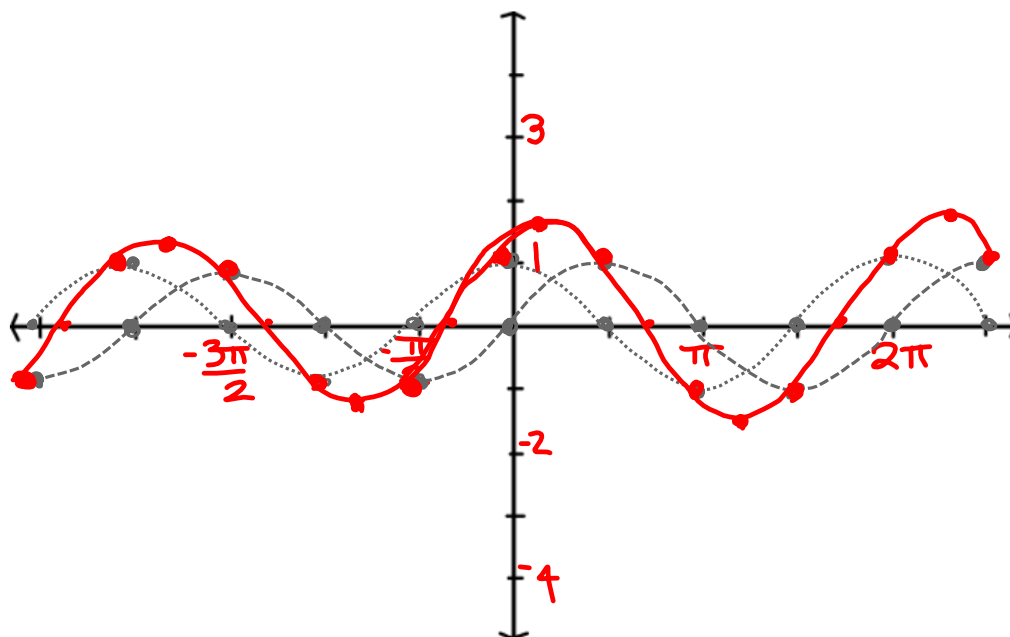
vert. shift:

up 1

$y = 2 \sin \frac{\pi}{3} x + 1$



$$y = \sin x + \cos x$$



#### Homework #4 (due Fri, 9/5)

- Graphing worksheets, problems #1-60
- 5.5 #55-60 all write an equation given a graph (sin & cos)  
#77-84 all write an equation given amplitude and period
- 5.6 #49-54 all write an equation given a graph (tan, cot, sec, csc)  
#63-70 all write an equation given ("amplitude" 1 and) period
- 5.7 #53-58 all graph sum functions  
#59-64 all write an equation given a graph  
#87-92 all write an equation given amplitude, period, & shifts