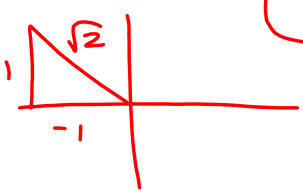


Assignments for the Week of Oct. 3

- Read 6.5, 6.6
- 45 minutes of Khan Academy
- Textbook assignment **due** Test Day:  
6.3 #1-24 all; 30-36 all; 49-93 odd
- **TEST #3**  
**9:00 class - Tues. 10/4**  
**8:00 class - Wed. 10/5**

Coming up after the test:

- 6.5 #1-24 all, #25-55 odd      Inverse Trig Functions
- 6.6 Solving Trig Equations

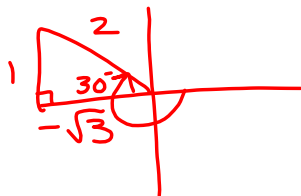
$$\cos \frac{27\pi}{4} = \cos \frac{3\pi}{4} = \frac{-1}{\sqrt{2}} = \frac{-\sqrt{2}}{2}$$


$$\frac{27\pi}{4} - 3 \cdot \frac{8\pi}{4} = \frac{3\pi}{4}$$

$$\begin{aligned}
 \tan 15^\circ &= \tan(45^\circ - 30^\circ) \\
 &= \frac{\tan 45^\circ - \tan 30^\circ}{1 + \tan 45^\circ \tan 30^\circ} \\
 &= \frac{1 - \frac{\sqrt{3}}{3}}{1 + 1 \cdot \frac{\sqrt{3}}{3}} = \frac{3 - \sqrt{3}}{3 + \sqrt{3}} = \frac{3 - \sqrt{3}}{3} \cdot \frac{3}{3 + \sqrt{3}} \\
 &= \frac{3 - \sqrt{3}}{3 + \sqrt{3}} \cdot \frac{3 - \sqrt{3}}{3 - \sqrt{3}} = \frac{9 - 6\sqrt{3} + 3}{9 - 3} = \\
 &= \frac{12 - 6\sqrt{3}}{6} = \frac{6(2 - \sqrt{3})}{6} = \boxed{2 - \sqrt{3}}
 \end{aligned}$$

$$\begin{aligned}
 \tan 15^\circ &= \tan \frac{30^\circ}{2} = \frac{1 - \cos 30^\circ}{\sin 30^\circ} = \\
 &= \frac{1 - \frac{\sqrt{3}}{2}}{\frac{1}{2}} = \left(1 - \frac{\sqrt{3}}{2}\right) \cdot \frac{2}{1} = \boxed{2 - \sqrt{3}}
 \end{aligned}$$

$$\sec\left(-\frac{7\pi}{6}\right) = -\frac{2}{\sqrt{3}} = \boxed{\frac{-2\sqrt{3}}{3}}$$



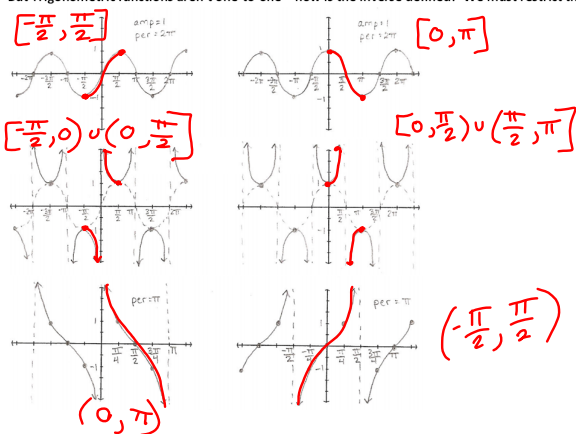
$$\sec\left(-\frac{7\pi}{6}\right) = \sec \frac{7\pi}{6} = \frac{1}{\cos \frac{7\pi}{6}} = \frac{1}{-\frac{\sqrt{3}}{2}} = \frac{-2}{\sqrt{3}} \dots$$

$$\begin{aligned}
 \sin 15^\circ &= \sin \frac{30^\circ}{2} = + \sqrt{\frac{1 - \cos 30^\circ}{2}} \\
 &= \sqrt{\frac{1 - \frac{\sqrt{3}}{2}}{2}} = \sqrt{\frac{\frac{2 - \sqrt{3}}{2}}{\frac{2}{1}}} \\
 &= \sqrt{\frac{2 - \sqrt{3}}{2} \cdot \frac{1}{2}} = \frac{\sqrt{2 - \sqrt{3}}}{\sqrt{4}} = \boxed{\frac{\sqrt{2 - \sqrt{3}}}{2}}
 \end{aligned}$$

$$\tan 2x = \frac{2 \sin x \cos x}{\cos^2 x - \sin^2 x}$$

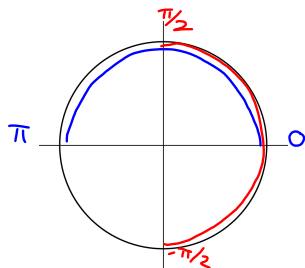
$$\begin{aligned}
 \text{LHS} = \tan 2x &= \frac{\sin 2x}{\cos 2x} = \frac{2 \sin x \cos x}{\cos^2 x - \sin^2 x} \\
 &= \text{RHS}
 \end{aligned}$$

But Trigonometric functions aren't one-to-one – how is the inverse defined? We must restrict the domain!



Summary of Restricted Domains:

Interval	Functions	Quadrants
$(-\frac{\pi}{2}, \frac{\pi}{2})$	$\sin x, \csc x, \tan x$	<u>IV &amp; I</u>
$(0, \pi)$	$\cos x, \sec x, \cot x$	<u>I &amp; II</u>

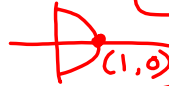


Evaluate.

$$\cot^{-1}\left(-\frac{1}{\sqrt{3}}\right) = \overset{120^\circ}{\boxed{\frac{2\pi}{3}}}$$



$$\tan^{-1}(0) = \boxed{0}$$



$$\sin^{-1}\left(\frac{\sqrt{3}}{2}\right) = \boxed{\frac{\pi}{3}}$$



$$\cos^{-1}(3) = \text{undefined}$$



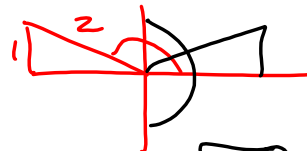
$$\csc^{-1}(-2) = \boxed{-\frac{\pi}{6}}$$



What happens when we compose a Trigonometric function with its inverse?

According to the definition,

$f(x)$  and  $g(x)$  are inverses if  $f(g(x)) = x$  and  $g(f(x)) = x$  (for all  $x$ -values in the respective domains of  $g$  and  $f$ )



We would then expect

$$\sin(\sin^{-1} x) = x \text{ and } \sin^{-1}(\sin x) = x$$

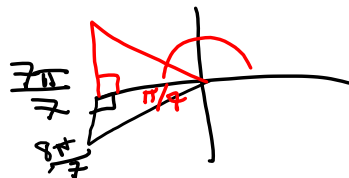
$$\sin\left(\sin^{-1}\frac{1}{2}\right) = \boxed{\frac{1}{2}}$$

$$\sin^{-1}\left(\sin\left(\frac{5\pi}{6}\right)\right) = \sin^{-1}\left(\frac{1}{2}\right) = \boxed{\frac{\pi}{6}}$$

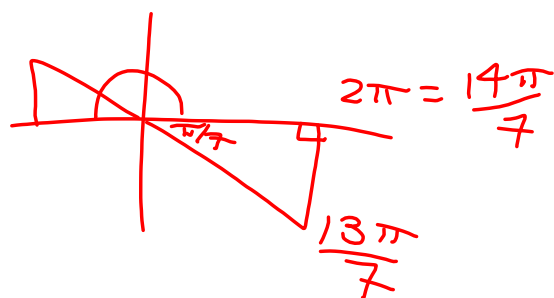
$$\sin^{-1}\left(\sin\left(-\frac{\pi}{6}\right)\right) = \boxed{-\frac{\pi}{6}}$$

$$\cos^{-1}\left(\cos\left(\frac{8\pi}{7}\right)\right) = \boxed{\frac{6\pi}{7}}$$

$$\sin(\sin^{-1} 3) = \text{undefined}$$



$$\cot^{-1}\left(\cot\frac{13\pi}{7}\right) = \boxed{\frac{6\pi}{7}}$$



Evaluate:

$$\cos^{-1}\left(\cos\left(\frac{12\pi}{7}\right)\right) = \boxed{\frac{2\pi}{7}}$$

$$\tan^{-1}\left(\tan\left(\frac{4\pi}{5}\right)\right) = \boxed{-\frac{\pi}{5}}$$

$$\sec^{-1}\left(\sec\left(-\frac{4\pi}{5}\right)\right) = \boxed{\frac{4\pi}{5}}$$

