

Assignments for the Week of Oct. 3

- Read 6.6, 7.1
- 45 minutes of Khan Academy
- Textbook assignment due Friday 10/14:
 - 6.5 #25-55 odd Inverse Trig Functions
 - 6.6 #1-21 odd Solving Trig Equations
 - #61-83 odd

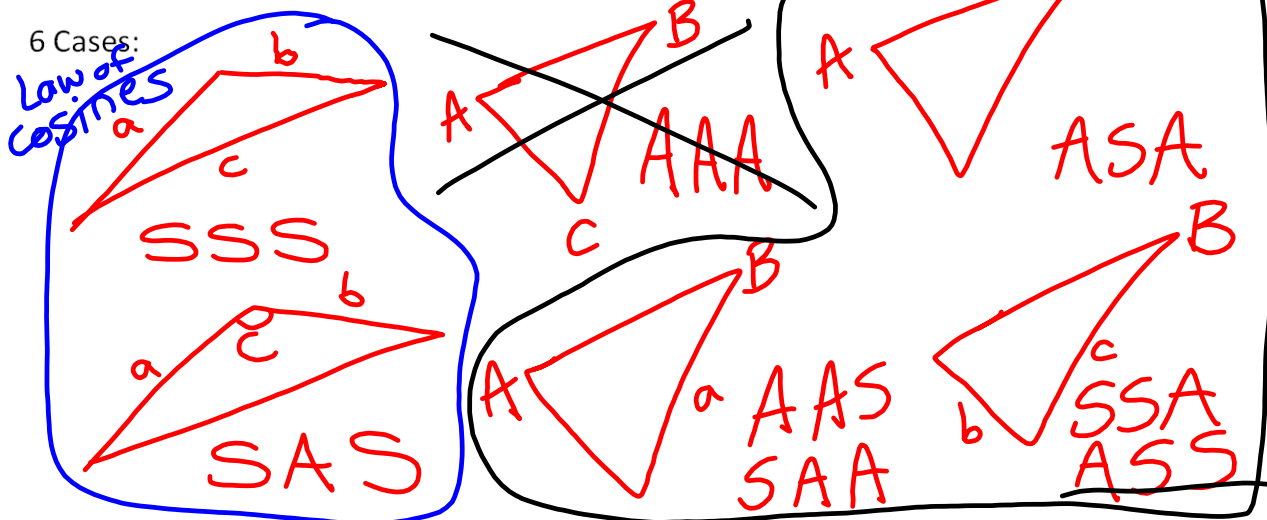
- Upcoming:
 - 7.1 Law of Sines
 - 7.2 Law of Cosines

Math Team Captain:
Maria Trifas

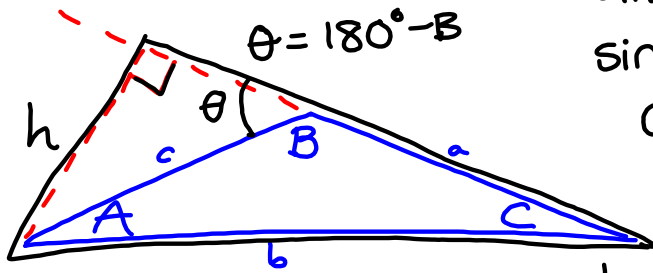
7.1 The Law of Sines

How do we solve oblique (not right) triangles?

6 Cases:



Derivation of the Law of Sines



$$\begin{aligned} \sin(180^\circ - B) &= \\ \sin 180^\circ \cos B - \cos 180^\circ \sin B &= \\ 0 \cdot \cos B - (-1) \sin B &= \\ &= \sin B \end{aligned}$$

$$\begin{aligned} \sin C &= \frac{h}{b} & \sin \theta &= \frac{h}{c} \\ b \sin C &= h & \sin B &= \frac{h}{c} \\ & & c \sin B &= h \end{aligned}$$

$$\begin{aligned} \frac{\cancel{b} \sin C}{\cancel{bc}} &= \frac{\cancel{c} \sin B}{\cancel{bc}} \\ \frac{\sin C}{c} &= \frac{\sin B}{b} \end{aligned}$$

$$\begin{aligned} \frac{\cancel{b} \sin C}{\cancel{\sin B} \cancel{\sin C}} &= \frac{\cancel{c} \sin B}{\cancel{\sin B} \cancel{\sin C}} \\ \frac{b}{\sin B} &= \frac{c}{\sin C} \end{aligned}$$

The Law of Sines

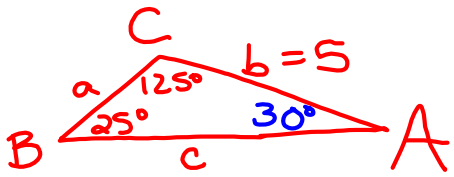
$$\frac{\sin A}{a} = \frac{\sin B}{b} = \frac{\sin C}{c}$$

or

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

7.1

2. $B=25^\circ$, $C=125^\circ$, $b=5$

AAS \rightarrow Law of Sines

$$\angle A = 180^\circ - 125^\circ - 25^\circ$$

$$\boxed{\angle A = 30^\circ}$$

$$\frac{a}{\sin A} = \frac{b}{\sin B}$$

$$\frac{a}{\sin 30^\circ} = \frac{5}{\sin 25^\circ}$$

$$a = \frac{5 \sin 30^\circ}{\sin 25^\circ}$$

$$\boxed{a \approx 5.9}$$

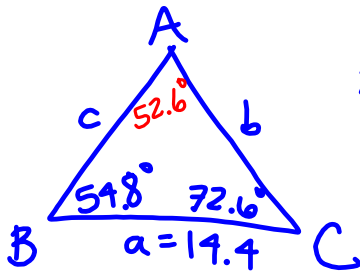
$$\frac{c}{\sin C} = \frac{b}{\sin B}$$

$$\frac{c}{\sin 125^\circ} = \frac{5}{\sin 25^\circ}$$

$$c = \frac{5 \sin 125^\circ}{\sin 25^\circ}$$

$$\boxed{c \approx 9.7}$$

8. $B=54.8^\circ$, $C=72.6^\circ$, $a=14.4$

ASA \rightarrow Law of Sines

$$\angle A = 180^\circ - 54.8^\circ - 72.6^\circ$$

$$\boxed{\angle A = 52.6^\circ}$$

$$\frac{b}{\sin 54.8^\circ} = \frac{14.4}{\sin 52.6^\circ}$$

$$b = \frac{14.4 \sin 54.8^\circ}{\sin 52.6^\circ}$$

$$\boxed{b \approx 14.8}$$

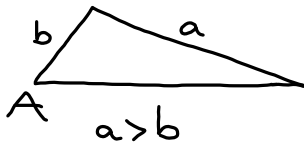
$$\frac{c}{\sin 72.6^\circ} = \frac{14.4}{\sin 52.6^\circ}$$

$$c = \frac{14.4 \sin 72.6^\circ}{\sin 52.6^\circ}$$

$$\boxed{c \approx 17.3}$$

ASS, The Problematic Triangle

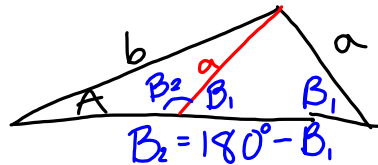
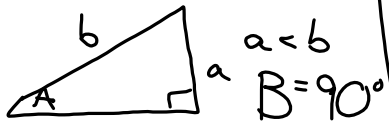
one solution:



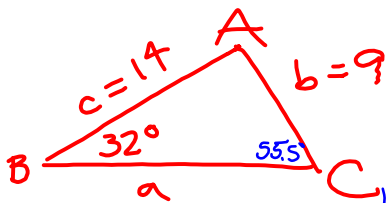
no solutions:



two solutions: $a < b$



14. $B = 32^\circ, c = 14, b = 9$



ASS \rightarrow Law of Sines
problematic - 0, 1, or 2 solutions

$$\angle A = 180^\circ - 32^\circ - 55.5^\circ$$

$$\angle A \approx 92.5^\circ$$

$$\frac{a}{\sin A} = \frac{b}{\sin B}$$

$$\frac{a}{\sin 92.5^\circ} = \frac{9}{\sin 32^\circ}$$

$$a = \frac{9 \sin 92.5^\circ}{\sin 32^\circ}$$

$$\frac{\sin C}{c} = \frac{\sin B}{b}$$

$$\frac{\sin C}{14} = \frac{\sin 32^\circ}{9}$$

$$\sin C = \frac{14 \sin 32^\circ}{9}$$

$$C = \sin^{-1}\left(\frac{14 \sin 32^\circ}{9}\right)$$

$$a \approx 17.0$$

$$C_1 \approx 55.5^\circ$$

7.1 The Law of Sines, continued

ASS – Problematic Triangle

14. $B = 32^\circ, c = 14, b = 9$

Case 1: $C \approx 55.5^\circ, A \approx 92.5^\circ, a \approx 17$

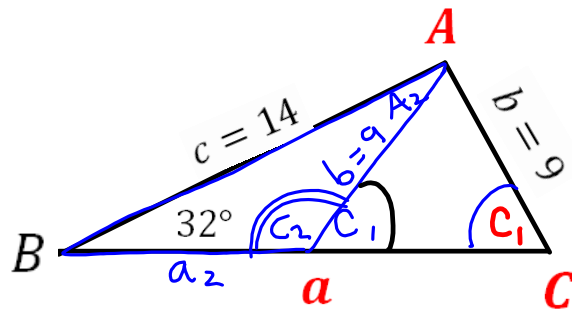
$$C_2 = 180^\circ - C_1$$

$$= 180^\circ - 55.5^\circ$$

$$C_2 = 124.5^\circ$$

$$A_2 = 180^\circ - 32^\circ - 124.5^\circ$$

$$A_2 \approx 23.5^\circ$$



$$\frac{a_2}{\sin A_2} = \frac{9}{\sin 32^\circ}$$

$$a_2 = \frac{9 \sin(23.5^\circ)}{\sin 32^\circ}$$

$$a_2 = 6.8$$