

$$24. f(x) = \frac{1}{2}x^3 + 2$$

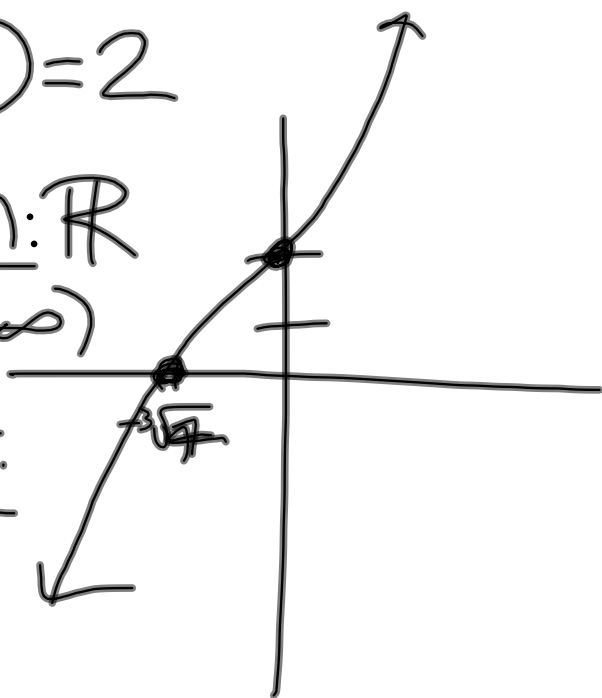
$$f(0) = 2$$

domain: \mathbb{R}

$(-\infty, \infty)$

range:

\mathbb{R}



A hand-drawn graph of the function $f(x) = \frac{1}{2}x^3 + 2$. The graph shows a curve passing through the origin $(0, 0)$ and the x-axis at a point labeled with a cube root symbol $\sqrt[3]{-4}$. The curve is increasing and concave up.

$$\frac{1}{2}x^3 + 2 = 0$$

$$\frac{1}{2}x^3 = -2$$

$$x^3 = -4$$

$$x = \sqrt[3]{-4}$$

$$27. \quad g(t) = 2 \sin \pi t \quad \text{amp: } 2$$

$$\text{per: } \frac{2\pi}{\pi} = 2$$



$$\text{domain: } \mathbb{R}$$
$$\text{range: } [-2, 2]$$

$$18. f(x) = \begin{cases} x^2 + 2, & x \leq 1 \\ 2x^2 + 2, & x > 1 \end{cases}$$

$$(a) f(-2) = (-2)^2 + 2 = 6$$

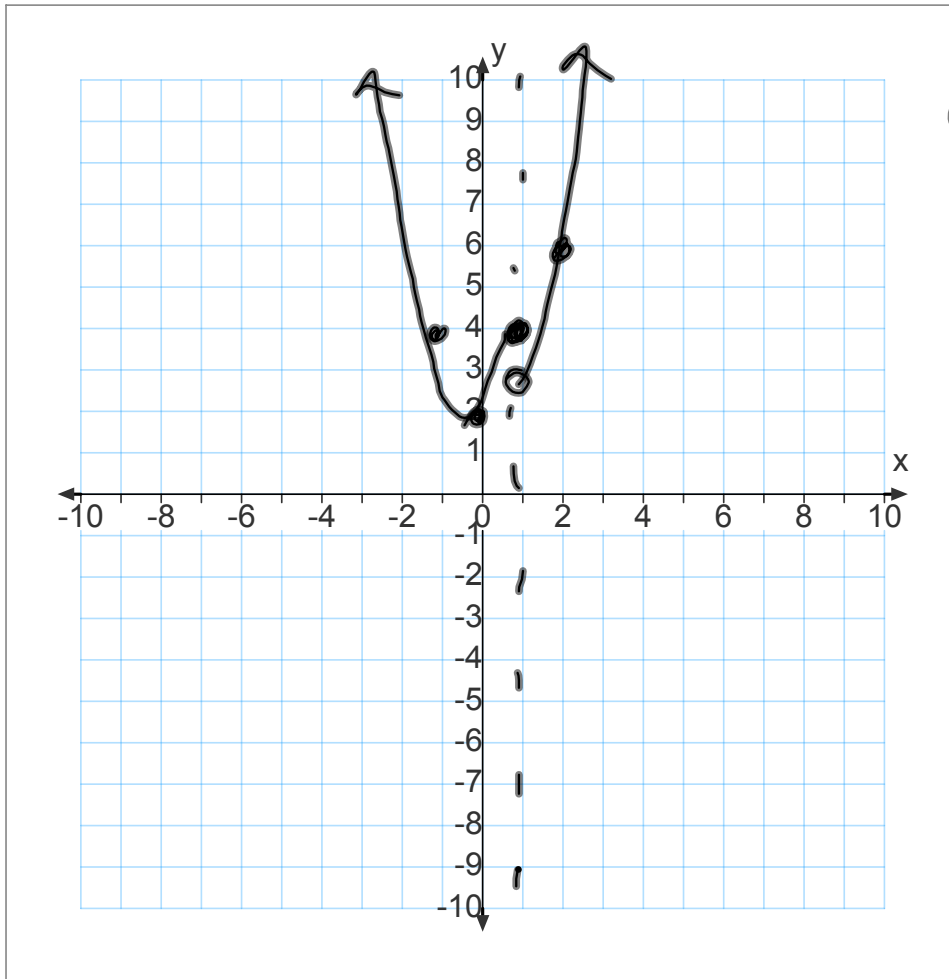
$$(b) f(0) = 0^2 + 2 = 2$$

$$(c) f(1) = 1^2 + 2 = 3$$

$$(d) f(s^2 + 2) = 2(s^2 + 2)^2 + 2 = 2(s^4 + 4s^2 + 4) + 2 = 2s^4 + 8s^2 + 10$$

domain: \mathbb{R}

range: $[2, \infty)$



$$\begin{cases} 2x^2 + 2, & x \leq 1 \\ x^2 + 2, & x > 1 \end{cases}$$

Δx "delta x"
change in x

$f(x + \Delta x)$

$$\frac{f(x+h) - f(x)}{h}$$

Δx

Δx

1.2

$$f(x) = \frac{x-2}{x^2-4}, \quad x \neq 2, -2$$

what happens to $f(x)$ as x approaches 2?

x	1.9	1.99	1.999	2	2.001	2.1
$f(x)$	0.2564	0.2506	0.2501	?	0.2499	0.2439

$f(x) \rightarrow 0.25$ as $x \rightarrow 2$.

Informal Description of the Limit

If $f(x)$ becomes arbitrarily close to a single number L as x approaches c from either side, the limit of $f(x)$, as x approaches c , is L .

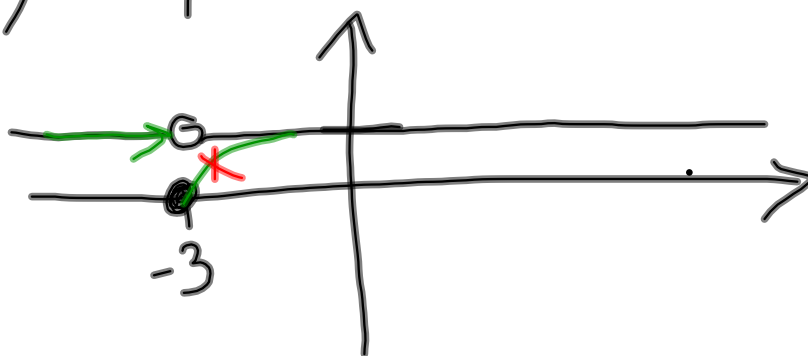
$$\lim_{x \rightarrow c} f(x) = L$$

Note: the existence or nonexistence of $f(x)$ at $x=c$ has no bearing on the existence of the limit as $x \rightarrow c$.

$$\lim_{x \rightarrow -3} \frac{\sqrt{1-x} - 2}{x+3} = -0.25$$

$$f(x) = \begin{cases} 1, & x \neq -3 \\ 0, & x = -3 \end{cases} \quad f(-3) = 0$$

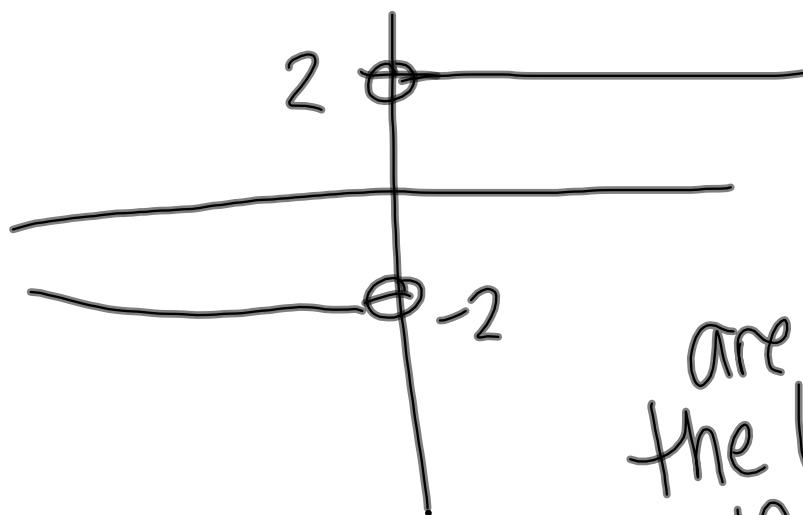
$$\lim_{x \rightarrow -3} f(x) = 1$$



$$\lim_{x \rightarrow 0} \frac{|2x|}{x}$$

$$|x| = \begin{cases} x, & x \geq 0 \\ -x, & x < 0 \end{cases}$$

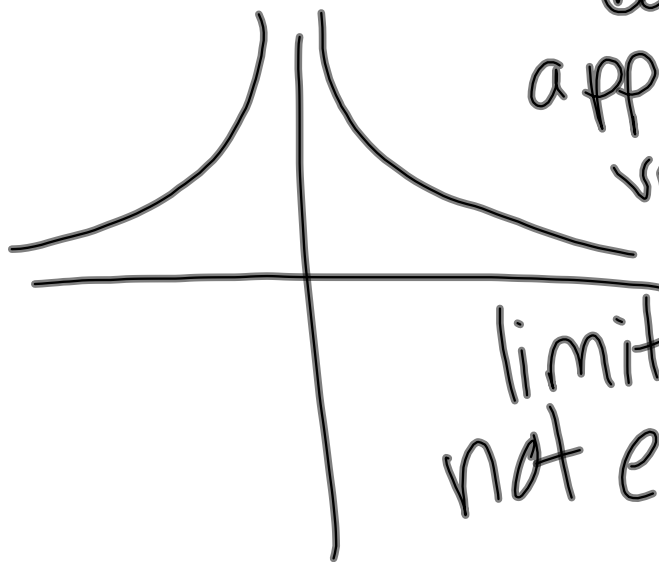
$$\frac{|2x|}{x} = \begin{cases} \frac{2x}{x} = 2, & x > 0 \\ \frac{-2x}{x} = -2, & x < 0 \end{cases}$$



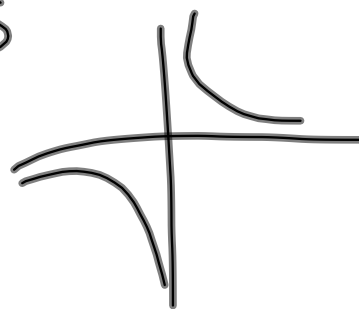
since
right &
left limits
are different,
the limit does
not exist.


$$\lim_{x \rightarrow 0} \frac{1}{x^4}$$

because $f(x)$ increases without bound (does not approach a finite value), $\frac{1}{x^{\infty}}$

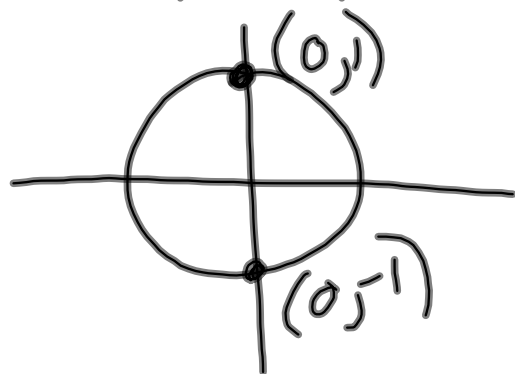


limit does not exist.



$$\lim_{x \rightarrow 0} \sin \frac{1}{x}$$


x	$\frac{2}{\pi}$	$\frac{2}{3\pi}$	$\frac{2}{5\pi}$	$\frac{2}{7\pi}$	$\frac{2}{9\pi}$	$\frac{2}{11\pi}$
$\sin \frac{1}{x}$	1	-1	1	-1	1	-1

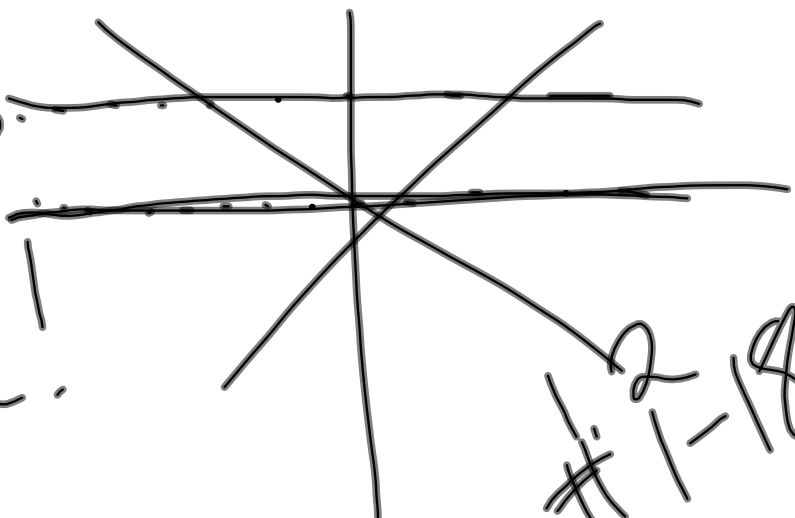


limit does
not exist as $x \rightarrow 0$
b/c function oscillates

"Dirichlet Function"

$$f(x) = \begin{cases} 0, & \text{if } x \text{ is rational} \\ 1, & \text{if } x \text{ is irrational} \end{cases}$$

limit does not exist anywhere!



#2-18