

1.2 # 1-5 odd

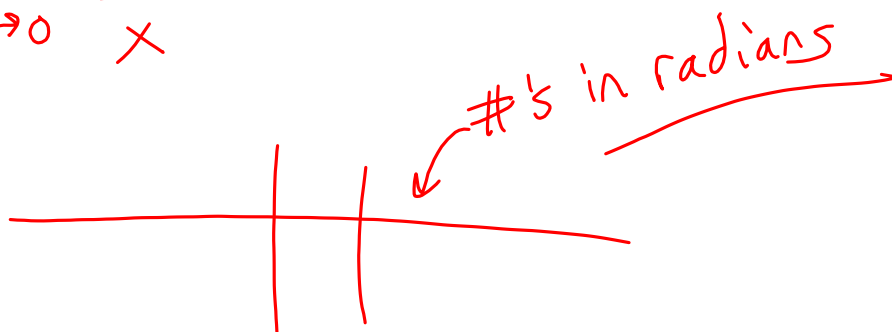
15-21 odd

23, 24

due Fri

37, 39, 41 → find  $\delta$

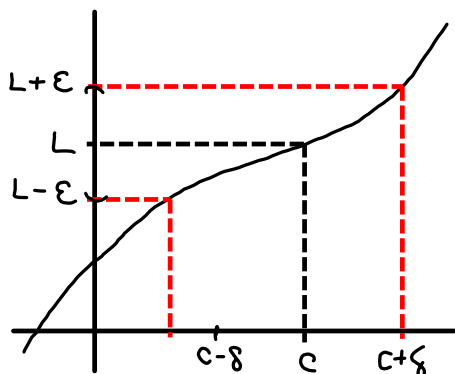
$$\lim_{x \rightarrow 0} \frac{\sin x}{x}$$



$\epsilon - \delta$  Definition of the Limit:

$\lim_{x \rightarrow c} f(x) = L$  if given  $\epsilon > 0$ , there exists a  $\delta > 0$  such that

$|f(x) - L| < \epsilon$  whenever  $0 < |x - c| < \delta$ .

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$f(x) = -5x + 3$ ; find  $\lim_{x \rightarrow 1} f(x)$  & find a  $\delta$ .

$$L = -2, c = 1$$

Let  $\epsilon > 0$  be given.

$$\begin{aligned} |f(x) - L| &= |-5x + 3 - (-2)| = |-5x + 5| \\ &= |-5(x - 1)| = 5|x - 1| < \epsilon \end{aligned}$$

$$|x - 1| < \boxed{\frac{\epsilon}{5} = \delta}$$

Prove that the limit is  $L$  using the  $\varepsilon - \delta$  definition of the limit

$$28. \lim_{x \rightarrow -3} (2x + 5) = 2(-3) + 5 = -1 = L$$

$\uparrow$   
 $c$

$$|2x + 5 - (-1)| = |2x + 6| = 2|x + 3| < \varepsilon$$

$x - (-3)$

$$|x + 3| < \frac{\varepsilon}{2} = \delta$$

Find  $\delta$  for  $\varepsilon = 0.01$

$$24. \lim_{x \rightarrow 4} \left(4 - \frac{x}{2}\right) = 4 - \frac{4}{2} = 4 - 2 = 2 = L$$

$\uparrow$   
 $c$

$$\left|4 - \frac{x}{2} - 2\right| = \left|-\frac{1}{2}x + 2\right| = \left|-\frac{1}{2}(x - 4)\right|$$

$$\varepsilon = 0.01$$

$$\Rightarrow \delta = 0.02$$

$$= \frac{1}{2}|x - 4| < \varepsilon$$

$$|x - 4| < 2\varepsilon = \delta$$

Find  $\delta$  for  $\varepsilon = 0.01$

$$26. \lim_{x \rightarrow 5} (x^2 + 4) = \underbrace{5^2 + 4}_{=c} = \underline{29} = L$$

Let  $\varepsilon > 0$  be given.

$$|f(x) - L| = |x^2 + 4 - 29| = |x^2 - 25| =$$

$$= |(x+5)(x-5)|$$

since  $x \rightarrow 5$   $4 < x < 6 \Rightarrow 9 < x+5 < 11$   
 $|x+5| < 11$

$$\Rightarrow |x+5| |x-5| < 11 |x-5| < \varepsilon$$

$$|x-5| < \frac{\varepsilon}{11} = \delta$$

Graph the rational function.

$$f(x) = \frac{(x+4)(x-1)}{(x-2)(x+1)}$$

Endbehavior:  $\frac{x^2}{x^2} = 1 = y$

$$\approx \frac{x^2 + \dots}{x^2 + \dots}$$

$$\lim_{x \rightarrow \infty} f(x) = 1$$

$$\lim_{x \rightarrow 2^-} f(x) = -\infty$$

$$\lim_{x \rightarrow 0} f(x) = 2$$

