

$$y = -x^2 + c$$

$$A(x) = 2x(-x^2 + c)$$

$$A(x) = -2x^3 + 2xc$$

$$A'(x) = -6x^2 + 2c$$

$$-6x^2 + 2c = 0$$

$$2c = 6x^2$$

$$\frac{c}{3} = x^2$$

$$\pm\sqrt{c/3} = x$$

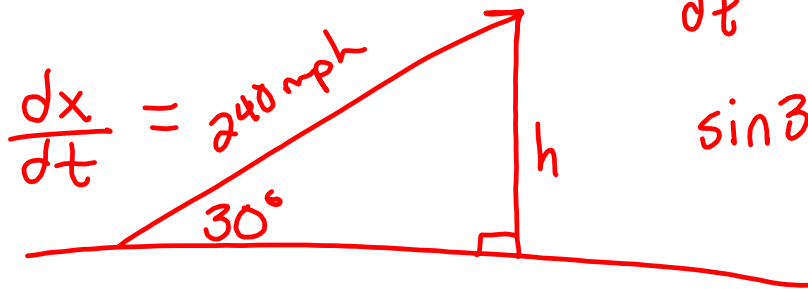
$$\text{width} = 2x$$

$$= 2\sqrt{c/3}$$

$$\text{height} = -x^2 + c$$

$$= -\frac{c}{3} + c = \frac{2c}{3}$$

12. An airplane is flying in still air with an airspeed of 240 miles per hour. If it is climbing at an angle of 30° , find the rate at which it is gaining altitude.



$$\frac{dh}{dt} = ? \quad \frac{dx}{dt} = 240$$

$$\sin 30^\circ = \frac{h}{x}$$

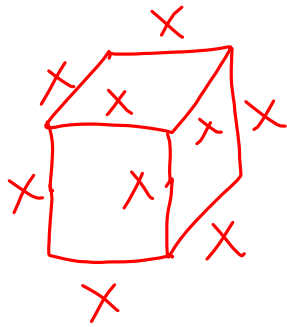
$$h = x \sin 30$$

$$h = \frac{x}{2}$$

$$\frac{dh}{dt} = \frac{1}{2} \frac{dx}{dt}$$

$$= \frac{1}{2} (240) = 120 \text{ mph}$$

10. All edges of a cube are expanding at a rate of 3 centimeters per second. How fast is the volume changing when each edge is 10 centimeters?



$$\frac{dx}{dt} = 3 \text{ cm/s} ; \frac{dV}{dt} = ? \text{ When } x = 10 \text{ cm}$$

$$V = x^3$$

$$\frac{dV}{dt} = 3x^2 \cdot \frac{dx}{dt} = 3(10)^2 \cdot (3)$$

$$= 900 \text{ cm}^3/\text{s}$$

17. Locate the absolute extrema on the closed interval.

$$f(x) = x^3 - 12x, \quad [0, 4]$$

18. Determine whether the Mean Value Theorem can be applied to f on the closed interval, and if so, find all

$$\text{values of } c \text{ such that } f'(c) = \frac{f(b) - f(a)}{b - a}.$$

$$f(x) = \frac{x+1}{x}, \quad \left[\frac{1}{2}, 2\right]$$

$$17. f'(x) = 3x^2 - 12$$

$$3(x^2 - 4) = 0$$

$$x = \pm 2$$

$$f(0) = 0$$

$$f(2) = 8 - 24 = -16 \leftarrow \text{abs min}$$

$$f(4) = 64 - 48 = 16 \leftarrow \text{abs max}$$

19. Find the critical numbers of f (if any), find the open intervals on which the function is increasing or decreasing, and locate all relative extrema.

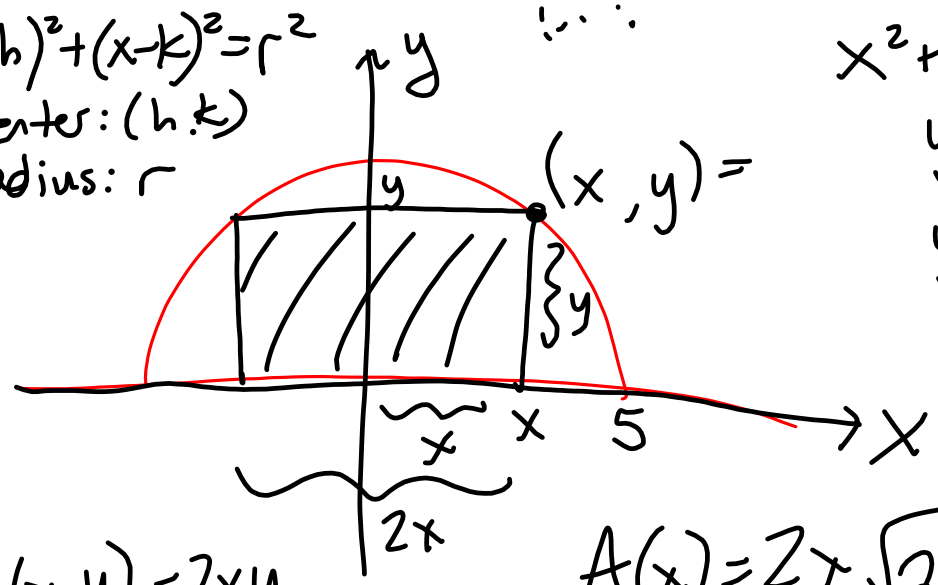
$$f(x) = \frac{x^2 - 2x + 1}{x + 1} \quad f'(x) = \frac{(x+1)(2x-2) - (x^2-2x+1) - 2x^2 - 2x + 2x - 2 - x^2 + x - 1}{(x+1)^2}$$

20. Find the points of inflection and discuss the concavity of the graph of the function.

$$f(x) = 2x^4 - 8x + 3$$

$f'(x) = 8x^3 - 8 = 8(x^3 - 1) = 8(x-1)(x^2+x+1)$
 $f''(x) = 24x^2 = 24x(x)$
 Critical points: $x = 1$
 Inflection points: $x = 0$
 $f(1) = 2(1)^4 - 8(1) + 3 = -3$
 $f(0) = 2(0)^4 - 8(0) + 3 = 3$
 Relative maximum at $(0, 3)$
 Relative minimum at $(1, -3)$
 Concave up on $(-\infty, 0) \cup (1, \infty)$
 Concave down on $(0, 1)$

$(x-h)^2 + (y-k)^2 = r^2$
 center: (h, k)
 radius: r



$x^2 + y^2 = 25$
 $y^2 = 25 - x^2$
 $y = \sqrt{25 - x^2}$

$A(x, y) = 2xy$

$A(x) = 2x\sqrt{25 - x^2}$