

24.  $\int_2^3 (x^2 + 5) dx$

1.  $\lim_{\|\Delta\| \rightarrow 0} \sum_{i=1}^n (c_i^2 + 5) \Delta x_i$

2.  $\lim_{\|\Delta\| \rightarrow 0} \sum_{i=1}^n c_i (2c_i^2 + 1) \Delta x_i$

$$= \int_2^3 (2x^2 + 1) dx$$

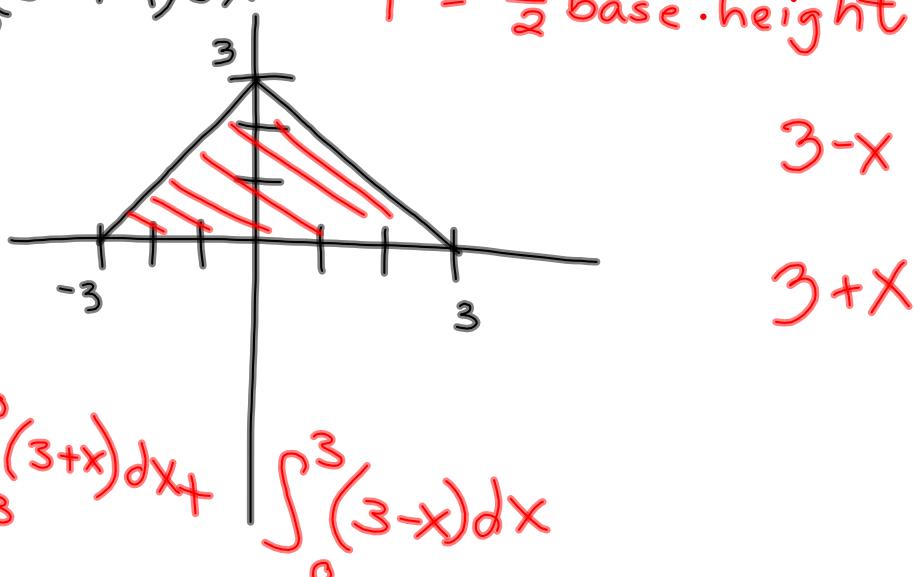
25.  $\int_0^3 f(x) = 5$ ,  $\int_3^7 f(x) = 11$

3)  $\int_7^0 f(x) dx = - \int_0^7 f(x) dx$

$$= - \left[ \int_0^3 + \int_3^7 \right] = -16$$

22.  $|x| = \begin{cases} x, & x \geq 0 \\ -x, & x < 0 \end{cases}$

$$\int_{-3}^3 (3 - |x|) dx = 9 = \frac{1}{2} \text{base} \cdot \text{height}$$



$$\int_{-3}^0 (3+x) dx + \int_0^3 (3-x) dx$$

20.  $\int_1^3 (2x+5) dx$

$$\begin{aligned} & \lim_{n \rightarrow \infty} \sum_{i=1}^n \left[ 2\left(1 + \frac{2i}{n}\right) + 5 \right] \cdot \frac{3-1}{n} \\ &= \lim_{n \rightarrow \infty} \frac{2}{n} \sum_{i=1}^n \left( 2 + \frac{4i}{n} + 5 \right) \\ &= \lim_{n \rightarrow \infty} \left[ \frac{2}{n} \sum_{i=1}^n 7 + \frac{8}{n^2} \sum_{i=1}^n i \right] \\ &= \lim_{n \rightarrow \infty} \left[ \frac{2}{n} \cdot 7n + \frac{8}{n^2} \cdot \frac{n(n+1)}{2} \right] \\ &= 14 + 4 = \boxed{18} \end{aligned}$$

$$\begin{aligned} \int_1^3 (2x+5) dx &= x^2 + 5x \Big|_1^3 = \\ (9+15) - (1+5) &= 24 - 6 = \boxed{18} \end{aligned}$$

4.1

70. balloon rises vertically  
 $\text{@ } 16 \text{ ft/s} = v(0) = s(0)$   
 releases sandbag  $64 \text{ ft above ground}$

(a) How many seconds after release will bag strike ground?

(b) @ what velocity will it hit ground?

$$a(t) = -32 \text{ ft/s}^2$$

$$v(t) = -32t + 16$$

$$s(t) = -16t^2 + 16t + 64$$

$$v(t) = a_0 t + v_0$$

$$s(t) = \frac{1}{2} a_0 t^2 + v_0 t +$$

$$(a) -16t^2 + 16t + 64 = 0$$

$$-16(t^2 - t - 4) = 0$$

$$t^2 - t - 4 = 0$$

$$t = \frac{1 \pm \sqrt{1-4(-1)(-4)}}{2} = \frac{1 \pm \sqrt{17}}{2}$$

$$\frac{1+\sqrt{17}}{2} \text{ s}$$

$\approx 2.56$

$$(b) v\left(\frac{1+\sqrt{17}}{2}\right) = -32\left(\frac{1+\sqrt{17}}{2}\right) + 16 \text{ ft/s} \approx -6$$

$$78. x(t) = (t-1)(t-3)^2, 0 \leq t \leq 5$$

(a) find  $a(t)$  &  $v(t)$

(b) find open  $t$ -intervals on which particle is moving to the right

(c) find  $v(t)$  when  $a(t) = 0$

$$\begin{aligned} x(t) &= (t-1)(t^2 - 6t + 9) \\ &= t^3 - 6t^2 + 9t - t^2 + 6t - 9 \\ &= t^3 - 7t^2 + 15t - 9 \end{aligned}$$

$$v(t) = 3t^2 - 14t + 15$$

$$a(t) = 6t - 14$$

$$\begin{aligned} 3t^2 - 14t + 15 & \\ 3t^2 - 9t - 5t + 15 & \\ 3t(t-3) - 5(t-3) & \\ (t-3)(3t-5) & \end{aligned}$$

$$\begin{array}{r} 3t^2 - 14t + 15 > 0 \\ 0 \quad | \quad 2 \quad | \quad 4 \\ + \frac{5}{3} - 3 + \end{array}$$

moving to the right on  $(0, \frac{5}{3}) \cup (3, 5)$

$$a(t) = 0 \text{ when } t = \frac{7}{3}$$

$$v\left(\frac{7}{3}\right) = 3\left(\frac{7}{3}\right)^2 - 14\left(\frac{7}{3}\right) + 15 = -\frac{4}{3}$$

4.1

$$58. f'(s) = 6s - 8s^3 \quad ; \quad f(2) = 3$$

$$f(s) = 3s^2 - 2s^4 + C$$

general solution

$$3 = 3(2)^2 - 2(2)^4 + C$$

$$C = 3 - 12 + 32 = 23$$

$$f(s) = 3s^2 - 2s^4 + 23$$

particular solution

4.4

1<sup>st</sup> Fundamental Theorem of Calculus

if  $F$  is antiderivative of  $f$ , &  $f$  is cts on

$$\int_a^b f(x) dx = F(b) - F(a)$$

$\therefore f$  is the derivative of  $F$   
 $F'(x) = f(x)$

Mean Value Theorem for Integrals

$$\int_a^b f(x) dx = f(c)(b-a)$$

if  $f$  is cts on  $[a, b]$   
 $\exists c \in (a, b)$  s.t.

## 2nd Fundamental Theorem of Calculus

If  $f$  is cts on open interval containing  $a$ ,

$$\frac{d}{dx} \left[ \int_a^x f(t) dt \right] = f(x)$$

**HW: #1-19**